

IN THE CLAIMS

1. (Currently Amended) A method of estimating carrier frequency offset error in a received sample bit stream including an observation vector (OV), having an observed carrier frequency timing offset ϵ , and a plurality of data-symbol frames, having a symbol timing offset error ϑ , comprising the steps of:

generating a probability density function (PDF) based on an extension portion and a synchronization portion of said OV, the PDF including first and second terms based on said symbol timing error ϑ ; and

generating from said PDF an estimate of carrier frequency offset error, $\epsilon_{MVU|\vartheta}$, being a minimum variance unbiased (MVU) estimator.

2. (Currently Amended) ~~The MVU carrier frequency offset error estimation method of claim 1 wherein said OV~~ extension portion comprises an L-bit cyclic extension portion and said synchronization portion comprises a first and a second N-bit synchronization frames, and wherein ~~said PDF comprises a~~ the first term, p1, based on said symbol timing offset error ϑ being within the span 1 to N and a the second term, p2, based on said symbol timing offset error ϑ being within the span N+1 to N+L.

3. (Currently Amended) ~~The MVU carrier frequency offset error estimation method of claim 2 wherein said received bit stream has uncorrelated independent identically distributed random signal and noise sequence variables with power of σ_s^2 and σ_n^2 , respectively, wherein said OV is denoted x , and wherein said MVU estimator $\epsilon_{MVU|\vartheta}$ is the conditional expectation of a second moment estimator, said second moment estimator given by~~

$$\tilde{\epsilon} = \frac{\Im}{2\pi} \ln \left\{ \frac{1}{L\sigma_s^2} \sum_{k=0}^{\vartheta+L-1} x[k]x^*[k+N] \right\}.$$

4. (Currently Amended) ~~The MVU carrier frequency offset error estimation method of claim 3 wherein said MVU estimator $\epsilon_{MVU|\vartheta}$ is given by~~

$$\tilde{\epsilon}_{MVU|\vartheta} = E(\tilde{\epsilon} | \mathcal{T}(\chi, \vartheta)) = \frac{\Im}{2\pi} \ln E \left\{ \frac{1}{L\sigma_s^2} \sum_{k=\vartheta}^{\vartheta+L-1} x[k]x^*[k+N] | \mathcal{T}(\chi, \vartheta) \right\}$$

$$= \frac{1}{2\pi} \Im \left\{ \ln \frac{T_1(\chi, \vartheta)}{L\sigma_s^2} \right\}$$

where \Im is the an imaginary operator and where

$$T_{1(\chi, \vartheta)} = \begin{cases} \sum_{k=\vartheta}^{L+\vartheta-1} x[k]x^*[k+N] & 1 \leq \vartheta \leq N \\ \sum_{k=0}^{\vartheta-N-1} x[k]x^*[k+N] + \sum_{k=\vartheta}^{N+L-1} x[k]x^*[k+N] & N+1 \leq \vartheta \leq N+L \end{cases}$$

5. (Currently Amended) A method of synchronizing a ~~received sample-bit stream~~, comprising the steps of:

~~transmitting at a transmitter said bit stream including an observation vector (OV);~~

~~receiving and sampling, at a receiver, said bit stream, said sampled bit stream including i) an observation vector (OV), said OV with having an observed carrier frequency offset ϵ , and ii) a plurality of data-symbol frames, having a symbol timing offset error ϑ ;~~

~~generating a probability density function (PDF) based on an extension portion and a synchronization portion of said OV, the PDF including first and second terms based on said symbol timing error ϑ ;~~

~~generating from said PDF an estimate of carrier frequency offset error, $\epsilon_{MVU|\vartheta}$, being a minimum variance unbiased (MVU) estimator; and~~

~~synchronizing said ~~received~~-bit stream by said MVU estimate of carrier frequency offset.~~

6. (Currently Amended) The ~~synchronization~~-method of claim 5 wherein said ~~OV-extension portion~~ comprises an L-bit cyclic extension portion and said synchronization portion comprises a first and a second N-bit synchronization frames, and wherein said ~~PDF comprises a first term, p1, based on said observed symbol timing offset error ϑ being within the span 1 to N and a said second term, p2, based on said observed symbol timing offset error ϑ being within the span N+1 to N+L.~~

7. (Currently Amended) The ~~synchronization~~-method of claim 6 wherein said ~~received~~-bit stream has uncorrelated independent identically distributed random signal and noise sequence variables with power of σ_s^2 and σ_n^2 , respectively, wherein said OV is denoted x , and wherein said MVU estimator $\epsilon_{MVU|\vartheta}$ is the conditional expectation of a second moment estimator, said second moment estimator given by

$$\tilde{\varepsilon} = \frac{\Im}{2\pi} \ln \left\{ \frac{1}{L\sigma_s^2} \sum_{k=\nu}^{\mathcal{G}+L-1} x[k]x^*[k+N] \right\}.$$

8. (Currently Amended) The ~~synchronization~~ method of claim 7 wherein said MVU estimator $\varepsilon_{\text{MVU}}|_{\mathcal{G}}$ is given by

$$\begin{aligned} \tilde{\varepsilon}_{\text{MVU}}|_{\mathcal{G}} &= E(\tilde{\varepsilon} | T_1(\chi, \mathcal{G})) = \frac{\Im}{2\pi} \ln E \left\{ \frac{1}{L\sigma_s^2} \sum_{k=\mathcal{G}}^{\mathcal{G}+L-1} x[k]x^*[k+N] T_1(\chi, \mathcal{G}) \right\} \\ &= \frac{1}{2\pi} \Im \left\{ \ln \frac{T_1(\chi, \mathcal{G})}{L\sigma_s^2} \right\} \end{aligned}$$

where \Im is the ~~an~~ imaginary operator and where

$$T_{1(\chi, \mathcal{G})} = \begin{cases} \sum_{k=\mathcal{G}}^{L+\mathcal{G}-1} x[k]x^*[k+N] & 1 \leq \mathcal{G} \leq N \\ \sum_{k=0}^{\mathcal{G}-N-1} x[k]x^*[k+N] + \sum_{k=\mathcal{G}}^{N+L-1} x[k]x^*[k+N] & N+1 \leq \mathcal{G} \leq N+L \end{cases}$$

9-19. (Canceled)